## RDCS423 Tutorial Problems #3 - Time Constraint Projection, Propagation and Real-Time Logic

1. Suppose we have a time constraint imposed on the invoker of a remote object as  $TC_{in}$  and a time constraint imposed by the invokee  $TC_{out}$ . Let the service to be invoked succeed  $TC_{in}$  by exactly  $\gamma$  time units.

If  $TC_{in} = \langle t_{\alpha}^{in}, t_{\beta}^{in} \rangle$  and  $TC_{out} = \langle t_{\alpha}^{out}, t_{\beta}^{out} \rangle$  using *meet* convex interval relations, show the relationship between  $t_{x}^{in}$ 's and  $t_{x}^{out}$ 's holds.

2. With the following time constraints  $TC_1$  and  $TC_2$ :

$$\begin{array}{lll} TC_1\colon \ T_{begin}\colon 1.0\to 1.6 & T_{end}\colon 1.4\to 2.0 & C_{Id}\colon 0.2\to 0.6 \\ TC_2\colon \ T_{begin}\colon 0.2\to 2.2 & T_{end}\colon 1.0\to 3.0 & C_{Id}\colon 0.8\to 1.8 \end{array}$$

draw the time constraint laxity windows for both constraints and propagate  $TC_1$  onto  $TC_2$ . What can be said about occurrence windows for  $TC_1 \prec TC_2$  and  $TC_1 \succ TC_2$ ? What regions define where  $TC_1$  and  $TC_2$  have a non-null intersection, and an accurate knowledge is required of all constraint begin and end times?

3. Given the following system specification:

A control panel with a button that when pushed must generate an action SAMPLE which must execute within 10 time units. The computation time of this SAMPLE action is at least 5 time units.

Produce a set of RTL axioms corresponding to the specification and reduce them to determine if this specification is realisable or not.

4. In addition to the system specification of the previous question, add the safety assertion:

If the transmitted information is displayed within 8 time units of the completion of action SAMPLE, then within 15 time units of pressing button 1, the requested information will be displayed.

Now augment the set of RTL axioms and reduce them to determine if the safety assertion is consistent with the system specification.